

how to solve Newton's Second Law problems with one object

1. Make a sketch of the object and its surroundings. When possible, draw \vec{v} .
2. Identify the question with a “?” and a symbol.
3. Check that all given units are SI units .
4. For symbolic problems, write down the “ given ” symbols.
FREE-BODY DIAGRAM
5. Identify the object you will apply Newton's Second Law to. This is usually the object whose mass is mentioned in the problem. Identify the instant or interval of time for which you are applying Newton's Second Law to the object.
6. Start a Free-Body Diagram for the object by drawing a vector for the object's weight .
7. Complete the Free-Body Diagram by drawing a force vector exerted by each thing that is touching the object . The diagram should include only the forces exerted <i>on</i> , not <i>by</i> , the object that you are focusing on. A surface may exert <i>both</i> a normal force <i>and</i> a frictional force.
FORCE TABLE
8. Write down axes with positive directions —usually, you should choose an axis that points in the object's direction of movement.
9. Start a Force Table . For each force in your Free Body Diagram, write down a number, symbol, or expression for the magnitude of the overall vector . If you are given a value for the magnitude of a force, use that value. Otherwise, if a force has a “special formula”, use that special formula to calculate or represent the magnitude. The forces with special formulas are weight, kinetic friction, and <i>maximum</i> static friction: $w = mg$, $f_k = \mu_k n$, $\max f_s = \mu_s n$ There are no special formulas for normal force or tension, or for static friction when the static friction is not assumed to be at its maximum. If a magnitude has no special formula and no given value, just represent the magnitude with a symbol.
10. Complete the Force Table by breaking each force into components . Always include a “+” or “-” sign on each nonzero component. Use the value, symbol, or expression for the overall magnitude from step 9 to calculate or represent the components.
NEWTON'S SECOND LAW EQUATIONS
11. Write the Newton's Second Law equations at the top of two adjacent columns: $\sum F_x = m a_x \qquad \sum F_y = m a_y$ Keep your later versions of the <i>x</i> - and <i>y</i> -equations organized in these two columns.
12. On the left side of the Newton's Second Law equations, add all the individual force components , including any negative signs, using the components from the Force Table.
13. On the right side of the equations, where possible, substitute specific values or symbols for the object's mass and for a_x and a_y . If an object is motionless in a component, or if an object moves with constant velocity in a component, then that component of its acceleration is 0.
14. When you have one equation with one unknown, or when you have two equations with two unknowns, you can use algebra to solve for the unknowns.
15. Check that you answered the right question, and answered all parts of the question, and that your answer makes sense. For numerical answers, check that you included units. For symbolic answers, check that your answer includes only the “given” symbols.